Flow characteristics of bottom outlets with moving gates

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ABSTRACT
This study investigates the discharge characteristics of a bottom outlet with a moving gate by Flow3D. Experimental results for a scale model outlet of the Aswan Dam, Egypt, were used. Two different flow features were found. Pressurized flow established if the flume was filled and then the gate was slowly opened. However, a free surface flow occurred if the gate was fully opened and the entire flume was slowly flooded with water. The numerical simulations successfully captured the two flow patterns as well as the discharges and water surface profiles. The discharges were predicted with sufficient accuracy using the first-order momentum advection scheme. In comparison with the $k-\varepsilon$ turbulence model, the Re-Normalization Group model yields the best agreement with the experiments. The model performed with similar accuracy for both model and prototype cases.

Keywords: Bottom outlet, CFD simulation, moving gate, three-dimensional model, VOF model

1 Introduction
Successful design and operation of hydraulic structures require effective and reliable tools to be applied to a variety of problems, including spillways, intakes, or bottom outlets. These flows share a complex character due to three-dimensional (3D) effects, surface waves, and air entrainment. The main concerns are related to accurate estimates of discharge coefficients, frictional losses, details of local flow patterns, position of the free surface, and air entrainment. Until recently, hydraulic scale model tests have served as principal approach. The latest improvements in Computational Fluid Dynamics (CFD) promote their use in place of scale models. For CFD to become reliable and acceptable as a design tool, the results must be carefully validated using experimental data. Recent CFD works concerning spillways are due to Olsen and Kjellesvig (1998), Unami et al. (1999), Ho et al. (2001, 2006), Savage and Johnson (2001a, 2001b), Bhajantri et al. (2007), Griffith et al. (2007), and Mehmet et al. (2009). Unami et al. (1999) developed a two-dimensional (2D) numerical model for spillway flows. They found a reasonable agreement with experimental data. Savage and Johnson (2001a, 2001b) presented a 2D simulation of flow over an ogee spillway using a commercial CFD code (Flow3D 2006). They found good agreement with experiments for both pressure and discharge. Ho et al. (2001) used Flow3D to model eight scaled physical models of spillway upgrade projects in Australia, successfully validating Flow3D against physical models. Griffith et al. (2007) extended the application of Flow3D to the stability analysis of Wanapum Spillway, located on Columbia River in Washington State. Having estimated pressures for the Probable Maximum Flood (PMF) condition, they concluded that the conventional stability analysis approach underestimated the sliding safety factor by 40–50%. All these studies confirm successful modelling of spillway flows by CFD.

A new CFD application to a bottom outlet structure with a moving gate is presented herein. Its objective was to investigate the flow features of the bottom outlet with a moving gate. In scale model tests, two different flow features were observed. Pressurized flow resulted if the flume was filled and then the gate was slowly opened, whereas a free surface flow appeared if the gate was fully opened and the entire flume was slowly flooded with water. The numerical simulations successfully captured these two flow features as well as the discharges and water surface profiles.

2 Experiments
The experiments dealt with the hydraulic model studies for determining the discharge capacity of one of the bottom outlets of Aswan Dam, Egypt, involving a movable gate (Cederwall and Bergh 1982). Two different flow features were found (Fig. 1):
(1) pressurized flow was found if the flume was filled and then the gate was slowly opened (Case 1), and (2) free surface flow if the gate was fully opened and the entire flume was slowly flooded with water (Case 2).

Note that $H_e$ is the upstream flow depth and $a$ the bottom outlet opening. The main model was partly made in plywood of smooth, painted walls, and partly in transparent plastic using a geometrical scale of 1:22. Its surface roughness was retained with a Manning coefficient $n = 0.013 \text{ m}^{-1/3} \text{s}$ corresponding to an equivalent roughness height of 0.72 mm, as computed from the Strickler formula (Townson 1991). The scale model was placed in a glass walled, recirculating hydraulic flume that is 0.6 m wide, 1.2 m deep, and 40 m long. The discharge was measured with a calibrated rectangular, sharp-crested weir to $\pm 5\%$. The downstream flow was always supercritical. The Froude law-based scales for velocity, discharge, and pressure were 1:22$^{1/2}$, 1:22$^{5/2}$, and 1:22, respectively. Figure 1 shows the cross-section of the lower intake portion. The upstream water levels were measured at $x = -0.3 \text{ m}$, where $x$ is the streamwise distance, using a pressure tap and two manometers of $\pm (0.1 \text{ to } 0.2) \text{ mm}$ accuracy. The water surface profiles were measured from outside along the glass wall using a ruler from $x = 0.18 \text{ to } x = 1.5 \text{ m}$. These records were less reliable and had an estimated accuracy of $\pm 3 \text{ mm}$. The velocity distributions and pressures were also measured at section I (Fig. 1). All measurements were taken along the centre line of symmetry, i.e. at $y = 0.159 \text{ m}$, where $y$ denotes spanwise distance. For velocity measurements, a miniature velocity meter of 8 mm diameter and $\pm 5 \text{ cm s}^{-1}$ accuracy was used. A Prandtl tube with an external diameter of 5 mm was used for static pressure measurements, involving a total error between 3% and 7%. The experiments were conducted for both fully opened and partially opened gates.

### 3 Numerical model

Flow3D, which is a general purpose CFD program for modelling multi-physics flow problems, heat transfer, and solidification, was used herein, based on the Finite-Volume Method to solve the full 3D Reynolds Averaged Navier–Stokes equations of fluid motion in Cartesian coordinates (Flow3D 2006). Flow3D was previously validated for different types of spillway flows (Ho et al. 2001, 2006, Savage and Johnson 2001a, 2001b, Griffith et al. 2007). The free surface is modelled using the Volume Of Fluid (VOF) method. The strength of Flow3D lies with its full implementation of the VOF model as opposed to Partial Volume Of Fluid. In Flow3D, to capture the model geometry and the obstacle in a rectangular domain, the Fraction Area/Volume Obstacle Representation (FA VOR) method was used in analogy to the VOF model (Hirt and Nichols 1981, Hirt and Sicilian 1985, Hirt 1992). The Re-Normalization Group (RNG) turbulence and the air-entrainment models were used; further, the $k$-$e$ turbulence model was also investigated.

#### 3.1 Model geometry and computational grid

The scale model geometry was reproduced using AUTOCAD. The number of grids in $(x,y,z)$ was varied in three different ranges, i.e. $175 \times 10 \times 75$, $280 \times 16 \times 120$, and $210 \times 16 \times 120$, corresponding to a uniform mesh size in the range of $0.01 - 0.016 \text{ m}$ in the $(x,y)$ directions. In vertical direction, two different mesh resolutions were used. Non-uniform grid spacing from 0.3 to 0.9 mm was used adjacent to the bottom wall of the outlet corresponding to a non-dimensional wall distance between 30 and 100. Above the boundary layer, the mesh size ranged from 0.01 to 0.016 m. A resolution of 0.016 m corresponds to $175 \times 10 \times 75$ (Fig. 2). It was impossible to obtain similar boundary layer grid resolutions for the prototype due to excessive grid points. The smallest possible grid size was 4 mm. To test grid dependency, the simulations were started with coarser grid sizes in the range 0.05 – 0.02 m. The flow symmetry along the centre plane was used to model half of the structure.

#### 3.2 Boundary conditions

The upstream boundary was defined as hydrostatic pressure with various prototype energy heads from $H_e = 105 – 113 \text{ m}$ (Table 1). In Case 1, hydrostatic pressure was defined by setting $H_e$. In Case 2, a transient value of $H_e$ was used. An
outflow boundary was set at the outlet where the flow was super-
critical. The inlet turbulence properties were defined in terms of
turbulent kinetic energy and dissipation rate (Dargahi 2004). The
turbulent length scale was taken as $L = 0.07L$ (Casey and Win-
tergerste 2000), where $L$ = relevant flow length, taken as the
mean flow depth or the hydraulic radius at section I. The accel-
eration of gravity was applied in the negative $z$-direction. The
wall roughness was set using the roughness height computed
from the Strickler formula.

3.3 Initial conditions

The initial conditions were defined differently for two cases. In
Case 1, a fluid region was defined upstream of the closed gate
that filled the entire upstream portion of the model, equal to $H_e$
(Table 1). The implementation of a static boundary condition
maintained a constant fluid height (energy head). Gradually
opening the gate, the fluid discharged into the model under the
force of gravity. In Case 2, the initial fluid region covered the
entire model to a depth of 2 cm. The void initial pressure was
set to the atmospheric pressure in both cases.

3.4 Modelling moving gate

The gate movement was modelled using the General Moving
Object (GMO) model that required the motion specification.
A linear translation in the negative $z$-direction was used herein.
To model moving objects, the GMO model also uses the
FAVOR method.

3.5 Numerical solver

The simulations were run using the implicit solver Generalized
Minimum Residual method (Flow3D 2006), which is highly
accurate and efficient for a wide range of problems. The selected
discretization method was the first-order momentum advection
formulation. However, for Case 1 ($H_e = 0.682$ m), simulations
were done using both first- and second-order discretizations for
both the scaled model and the prototype. The initial time step
was set to 0.003 s.

The transient flow simulations were done in both the model
and prototype scales for Cases 1 and 2, using $H_e = 105, 107,$
110, and 113 m (prototype scale). In Case 1, the gate was
raised gradually from its closed position at the same speed as
in the experiments, i.e. 0.67 m s$^{-1}$. The water then started to
flood the model, and the gate was completely opened within
60 s. To reach a steady-state solution, the simulations were con-
tinued for 320 s. For prototype simulations, the speed was scaled
up with time scale factor, i.e. 1:4.69. In Case 2, the height of the
initial fluid region was increased linearly at 2 s intervals until it
reached the required height after 60 s. The simulations were con-
tinued for 320 s. The discharge characteristics were also studied
for partial closure of the gate. These simulations were done for
$H_e = 113$ m at 10 different gate openings that were increased
at a rate of 10% in height (Fig. 1). The effects of the following
variables on the solution were studied:

1. equivalent roughness height varied between 0.3 and
0.72 mm (model scale), where the lower range corresponds
to a hydraulically smooth, and the upper to a rough surface
2. turbulent length scale varied between 0.073 and 0.338 m
(model scale)
3. choice of advection method (first and second orders)
4. influence of turbulence model ($k$-$e$ and RNG)
5. influence of both up- and downstream model lengths
6. grid dependency of results

Altogether 30 simulations were done to cover the two cases and
the numerical variables. The transient flow simulations were con-
tinued until steady state and solution convergence were reached.
For the scaled model simulations, 30–60 s were needed. The
results were inspected for discharges and kinetic energy. The dis-
charges at the inlet and outlet boundaries were monitored to cal-
culate the mass imbalance, defined as difference between the two
discharges normalized with the inlet discharge.

4 Results

The Flow3D simulation outputs were visualized graphically or
saved as text files. The RNG turbulence model was compared
with the experimental data, with a focus on discharges.
Limited measurements of flow velocities and pressures were
also used, which were taken at $y = 0.159$ m.

The numerical model successfully captured the pressurized
flow (Case 1) and free surface flow (Case 2). Figures 3 and 4
compare the measured and simulated water surface profiles for
both cases ($G_s$ denotes mesh size and $z_e$ elevation). The measure-
ments did not cover the entire model length. There is a good
agreement between the data set; however, the agreement is
better for $x > 0.8$ m because of a higher reliability and accuracy
in the measurements. The comparison is better defined using the
relative error by taking the difference between simulation and
experimental values and then dividing the results by the exper-
imental values. An error range between 0.25% and 3.5% was
found for both cases. Table 2 compares the measured and simu-
lated discharges for Cases 1 and 2 and also lists the relative mass

| $H_e$, reservoir level (m) | $Q$, discharge Case 1
| | (m$^3$ s$^{-1}$) |
| | $Q$, discharge Case 2
| | (m$^3$ s$^{-1}$) |

<table>
<thead>
<tr>
<th>Prototype</th>
<th>Model</th>
<th>Prototype</th>
<th>Model</th>
<th>Prototype</th>
<th>Model</th>
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<td>155</td>
<td>0.068</td>
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imbalances, resulting in good agreement with the experiments. The discharges are predicted within 1.4–4.6%. The relative mass imbalances were in the range of 0.5–1.5%. Figure 5 compares the simulated and measured discharges at $H_e = 113$ m for different gate openings. The discharges are normalized ($Q_n$) with discharge of the fully opened gate. The gate opening heights $w_n$ are normalized with $a$ (Fig. 1). The agreement with the experimental data is good, with a maximum error of $\pm 1.5\%$. Inclusion of air entrainment in the simulations did not affect the discharges.

![Figure 3](image3.png)

**Figure 3** Comparison between simulated ($\Diamond L = 0.073$ m, $G_e = 0.016$ m) and (+) measured water surface profiles, Case 1 for $H_e = 1.045$ m

![Figure 4](image4.png)

**Figure 4** Comparison between simulated ($\Diamond L = 0.073$ m, $G_e = 0.01$ m; $\Box L = 0.073$ m, $G_e = 0.016$ m; $\times L = 0.0338$ m, $G_e = 0.016$ m) and (+) measured water surface profiles, Case 2 for $H_e = 1.045$ m

![Figure 5](image5.png)

**Figure 5** Comparison between (—) simulated and (+) measured normalized discharges at normalized gate openings, Case 1, $H_e = 113$ m ($H_{e\text{model}} = 1.045$ m)

![Figure 6](image6.png)

**Figure 6** Comparison between simulated (◇ simulated scale model, ● simulated prototype) and measured velocity profile (+), section I, Case 2 for $H_e = 113$ m ($H_{e\text{model}} = 1.045$ m)

Velocity and static pressure distributions showed good agreement. Figure 6 compares the streamwise velocity $u$ profiles for Case 2 at section I (Fig. 1). The experimental data were upscaled to prototype scale. They are overestimated by 2.6%.

<table>
<thead>
<tr>
<th>Case</th>
<th>$H_e$ prototype scale (m)</th>
<th>Surface roughness (mm)</th>
<th>Discharge experiments ($m^3 \cdot s^{-1}$)</th>
<th>Mean discharge ($m^3 \cdot s^{-1}$)</th>
<th>Mass imbalance (%)</th>
<th>Relative error (%)</th>
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<tr>
<td>1</td>
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<td>0.72</td>
<td>0.069</td>
<td>0.067</td>
<td>0.64</td>
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<td></td>
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<tr>
<td>2</td>
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<td>0.063</td>
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<td>0.28</td>
<td>4.60</td>
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<td></td>
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<tr>
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<td></td>
<td>0.088</td>
<td>-0.14</td>
<td>4.10</td>
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<tr>
<td></td>
<td>113</td>
<td></td>
<td></td>
<td>0.098</td>
<td>0</td>
<td>4.60</td>
</tr>
</tbody>
</table>
The agreement is better in the boundary layer near the wall. The static pressure $P_s$ profile for Case 2 is compared with those of the experiments in Fig. 7. The agreement is good except at elevations below 93 m. However, for Case 1 (not shown), the pressures were overestimated by 10%. The inclusion of air entrainment in the simulations did not improve the agreement.

5 Discussion

The discharges are lower for free surface than for pressurized flow. Free surface flow separates from the upper edge of the bottom outlet (Fig. 4), because of the negative static pressure distribution (Fig. 7). In turn, the flow separation gives rise to an additional contraction coefficient $C_c$, which is the ratio of $a$ to the flow depth at section II (Fig. 1), based on

$$Q = ab \mu_d C_i \sqrt{2g(H_e - C_c a)}$$

in which $b$ represents width of bottom outlet; $g$, acceleration of gravity; and $\mu_d$, discharge coefficient. For $H_e = 113$ m, $C_c \cong 0.916$. The corresponding value for pressurized flow is $C_c = 1$, such that the discharge is reduced by a factor of 0.925, comparable to the ratio of the two discharges, i.e. 0.918 (214/233, Table 1).

Hydraulic structure models are often based on the Froude similitude. Reynolds number-related scale effects are introduced, as the prototype Reynolds number is normally much larger than that of the model. The increase in the Reynolds number can affect the velocity distribution and the boundary layer properties. To examine this issue, the numerical scale models were up-scaled to prototype sizes and the simulations for the entire water levels were repeated for both Cases 1 and 2. Table 3 shows the simulation results in terms of discharge. Comparing Table 2 with Table 3, both the relative error and the mass imbalance are reduced for the prototype cases. There is a general increase in discharges of about 1%. However, the data do not provide any definite evidence of scale effects. One possible issue is the effect of surface roughness. Table 3 considers a smooth surface identical to the scale model. To address this issue, eight new simulations were done for equivalent roughness heights in the range from 5 to 15 mm, covering finished concrete surfaces (0.3–3 mm) and rough concrete surfaces (3–10 mm). The results were found independent from the surface roughness for rough concrete surfaces. However, the discharges were reduced for the high surface roughness of 15 mm, due to higher friction losses.

For partial gate closure, the discharge varies with the square of gate opening, whereas for a fully opened gate, discharge varies with $H_e^{1/2}$. The choices of turbulent length scale, the advection method, and the turbulence model are three important issues in CFD simulations of hydraulic structures. Using a high turbulent length scale increases the dynamic viscosity, which leads to over-prediction of diffusion, thereby causing large changes in the free-surface profile. The common approach is to use a value equal to 7% of a typical flow length scale. In the present study, the length scale was varied between 0.073 and 0.388 m, corresponding to 7% of

### Table 3  Comparison between measured and simulated discharges at prototype scale

<table>
<thead>
<tr>
<th>Case</th>
<th>$H_e$ prototype scale (m)</th>
<th>Surface roughness (mm)</th>
<th>Discharge Experiments ($m^3 s^{-1}$)</th>
<th>Mean flow discharge Flow3D ($m^3 s^{-1}$)</th>
<th>Mass imbalance (%)</th>
<th>Relative error (%)</th>
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<tr>
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<td>216</td>
<td>-0.18</td>
<td>1.00</td>
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</table>

*Extended downstream length (from 55 to 80 m)*
the flow depth or the hydraulic radius based on \(H_e\) and \(a\) (Fig. 1). The simulated water surface profiles were then found independent of the turbulent length scale (Fig. 4). One possible explanation for this insensitivity is related to the flow type. In accelerating flows, Reynolds shear stresses and turbulent kinetic energy levels decrease along the boundary layer when compared with the flat boundary layer. Bottom outlet flow is an accelerating flow type with damping turbulence effects thereby limiting the effect of length scale.

The choice of advection method was investigated for Case 1 and \(H_e = 0.682\) m for both scale model and prototype. Using the first-order scheme, the relative error in predicting the discharge coefficient was found to be 2.5%. The error was reduced to 2% for the second-order scheme, but the CPU time significantly increased. The accuracy of the first-order scheme was therefore considered sufficient. Comparing the two turbulence models, the RNG model gave the results that are closest to those of the experimental data.

Increasing the upstream model extent did not improve the accuracy in predicting the discharges. This might be due to the choice of the hydraulic static pressure condition at the upstream model section. Velocity-based boundary conditions appear to be more sensitive to this extent. The flow condition at the downstream section was supercritical, thus increasing the downstream model length did not affect the results (Table 3). The possible reasons for discrepancies between the experimental and simulated results are experimental errors, errors in flow modelling, and errors in geometrical modelling:

1) **Experimental errors** The discharge measurements were more reliable because a simple, well-established method free from various instabilities and flow problems was used. The error range from 1.4% to 4.6% is comparable to 4.6% in discharge measurement. The simulated water surface profiles disagreed more from the experiments, especially in the confined region of the model. Water surface fluctuations caused by the flow separation at the edges were difficult to measure at the flume glass wall. Beyond the confined region, the water surface profiles had a smoother shape and thus were easier to measure. The errors in predicting the velocity and static pressure measurements are comparable to the experimental errors. One possible reason was uncertainties involved concerning the exact location of the measurement points. Pressure measurement could have been affected by the presence of air bubbles in the measuring device.

2) **Errors in flow modelling** are related to the numerical methods (discretization and iteration errors), boundary conditions, and the closure models. The mass imbalance reported can be related to this category. The Finite Volume Method is always conservative. However, the numerical errors associated with the discretization scheme for the convective term result in a difference between the in- and outflow (mass imbalance). The estimated total error is about 2%, including 0.5% error in using the first-order discretization scheme.

3) **Errors in geometrical modelling** involve the quality of model geometry. The transfer of the model drawings to a physical model may be more inaccurate than transferring the drawings to a CAD model. A mismatch in geometrical design between a CAD and a physical model can affect the boundary layer properties as well as the discharges. The latter modify the pressure and velocity distributions. The errors in this category are comparable to the first category.

### 6 Conclusions

Computational fluid dynamics is an effective tool in analysing free-surface flows of bottom outlets. Pressurized and free-surface flow features were accurately captured using the Volume Of Fluid method implemented in Flow3D. The transient flow features associated with a moving gate were successfully captured as well as the discharge characteristic for partial opening of the gate. The water surface profiles and the discharges were predicted within a relative small error range. The first-order momentum advection scheme gives sufficient accuracy for engineering purposes. The velocity and pressure distributions were predicted within a maximum error of 2.6% and 10%, respectively. The model performed with similar accuracy for both model and prototype cases.

### Acknowledgements

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### Notation

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<thead>
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<th>Symbol</th>
<th>Description</th>
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<tr>
<td>(a)</td>
<td>bottom outlet opening</td>
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<tr>
<td>(b)</td>
<td>contraction coefficient</td>
</tr>
<tr>
<td>(C_e)</td>
<td>width of bottom outlet</td>
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<tr>
<td>(g)</td>
<td>acceleration of gravity</td>
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<td>(G_s)</td>
<td>mesh size</td>
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<td>(H_e)</td>
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<td>(L)</td>
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<tr>
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<td>static pressure head</td>
</tr>
<tr>
<td>(Q)</td>
<td>flow discharge</td>
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<tr>
<td>(Q_n)</td>
<td>discharge normalized with discharge of fully opened gate</td>
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<td>(u)</td>
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<tr>
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<td>(\varphi_n)</td>
<td>gate opening height normalized with (a)</td>
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References


